UNIVERSITY OF CRAIOVA Faculty of Mathematics and Computer Science Department of mathematics Fundamental domain : Exact sciences Domain: Mathematics Master: Applied mathematics Form: Day classes Duration of studies: 2 years Academic year 2009-2010

Ergodic Theory of Dynamical Systems Syllabus

Course coordinator: Prof. dr. Constantin P. Niculescu Code: MA213 Second Cycle: MASTER Second Year, Semester 1, Course 42 hours, Seminar 14 hours No. of credits: 6 Domain: Mathematics Type: compulsory Category: speciality

Objectives: The presentation of some of the most important ergodic theorems and the illustration of these results by applications from number theory and dynamical systems.

Necessary background: Special topics in functional analysis, Real and complex analysis, Probability theory.

Evaluation: Exam (E).

Contents:

1. Dynamical systems with an invariant measure. Poincaré's recurrence. The Bogoliubov-Krylov theorem.

- 2. The ergodic theorems of von Neumann and Birkhoff. Weyl's ergodic theorem.
- 3. Mixing and ergodicity.
- 4. Metric entropy. Topological entropy. The variational principle.
- 5. Special classes of mappings. Piecewise monotonic mappings. Denjoy diffeomorphisms. Billiards.
- 6. Recurrence and its applications to combinatorics. The theorems of van der Waerden and Szemeredi.
- 7. The ergodic theorem of Oseledec. Liapunov exponents. Applications to chaotic dynamical systems.

Bibliography:

1. V.I. Arnold et A. Avez, *Problemes Ergodique de la Mecanique Classique*. Gauthier-Villars, Paris, 1967.

2. A. Boyarsky and P. Góra, *Laws of Chaos. Invariant Measures and Dynamical Systems in One Dimension*, Birkhäuser, 1997.

3. M. Gidea and C. Niculescu, *Chaotic Dynamical Systems*. *An Introduction*. Universitaria Press, Craiova, 2002.

- 4. R. Gologan, Applications of Ergodic Theory, Editura Tehnica, Bucharest, 1989 (Romanian)
- 5. R. Mańe, Ergodic Theory and Differentiable Dynamics, Springer-Verlag, 1987.
- 6. W. Parry, Topics in Ergodic Theory, Cambridge Univ. Press, 1980.
- 7. Ya. G. Sinai, *Topics in Ergodic Theory*, Princeton Univ. Press, Princeton N.J., 1994.
- 8. M. Viana, Dynamics: A Probabilistic and Geometric Perspective, Proceedings of the International
- Congress of Mathematicians, Vol. I (Berlin, 1998). Doc. Math. 1998, Extra Vol. I, 557-578 (electronic).
 P. Walters, *An Introduction to Ergodic Theory*, Springer-Verlag, New York, Heidelberg, Berlin, 1982.

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